

In[15]:= ClearAll["Global`\*"]

In[16]:= a[t\_] = Exp[t];

In[17]:= doffactor[d\_] =  $\frac{d(d-3)}{2} + (d-2)$ ; (\*factor related to the degrees of freedom\*)

myH1[x\_, d\_, t\_] = HankelH1[ $\frac{d-1}{2}$ , x a[t]<sup>-1</sup>];

myHP1[x\_, d\_, t\_] = D[myH1[x, d, t], t];

myH2[x\_, d\_, t\_] = HankelH2[ $\frac{d-1}{2}$ , x a[t]<sup>-1</sup>];

myHP2[x\_, d\_, t\_] = D[myH2[x, d, t], t];

myBeta[x\_, d\_, t\_] =

$-I \left( \left( \frac{\text{Pi}}{8x} \right)^{\frac{1}{2}} \right) a[t]^{-\left(\frac{d-1}{2}\right)} \text{Exp}[I x] \left( \text{myHP2}[x, d, t] + \left( -I x - \frac{d-1}{2} \right) \text{myH2}[x, d, t] \right)$ ;

myBetastar[x\_, d\_, t\_] =  $I \left( \left( \frac{\text{Pi}}{8x} \right)^{\frac{1}{2}} \right) a[t]^{-\left(\frac{d-1}{2}\right)} \text{Exp}[-I x]$

$\left( \text{myHP1}[x, d, t] + \left( I x - \frac{d-1}{2} \right) \text{myH1}[x, d, t] \right)$ ;

myBetasqr[x\_, d\_, t\_] = Re[(myBeta[x, d, t]) (myBetastar[x, d, t])];

NumberDensity[x\_, d\_, t\_] =  $\frac{\text{myBetasqr}[x, d, t]}{(2 \text{Pi})^{(d-1)}}$ ;

BE[x\_] =  $\frac{1}{(\text{Exp}[x] - 1)}$ ;

intfactor[x\_, d\_] =  $\frac{2 \left( (\text{Pi})^{\frac{d-1}{2}} \right)}{\text{Gamma}\left[\frac{d-1}{2}\right]} (x^{(d-2)})$ ;

(\*factor related to the integration in d dimension\*)

EnergyDensity[d\_, t\_] =

NIntegrate[x (NumberDensity[x, d, t]) (BE[x]) (intfactor[x, d]), {x, 0, Infinity}];

NIntegrate::inumr : The integrand

$\left( 2^{-1-d} \pi^{2+\frac{1}{2}(-1+d)-d} x^{-1+d} \text{Re}\left[1/x(e^t)^{1-d} (\ll 1 \gg) \left( -\frac{1}{2} e^{-t} x (\text{HankelH2}[\text{Plus}[\ll 2 \gg], \text{Times}[\ll 2 \gg]] - \right. \right. \right.$   
 $\left. \left. \text{HankelH2}[\ll 2 \gg] + \left( \frac{1}{2} \text{Plus}[\ll 2 \gg] - i x \right) \text{HankelH2}\left[\frac{1}{2} \text{Plus}[\ll 2 \gg], \text{Power}[\ll 2 \gg] x\right] \right) \right] \right) / \left( \right.$   
 $\left. -1 + e^x \right) \text{Gamma}\left[\frac{1}{2}(-1+d)\right]$  has evaluated to

non-numerical values for all sampling points in the region with boundaries {{∞, 0}}. >>

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 $\left. \left. \text{HankelH2}[\ll 2 \gg] + \left( \frac{1}{2} \text{Plus}[\ll 2 \gg] - i x \right) \text{HankelH2}\left[\frac{1}{2} \text{Plus}[\ll 2 \gg], \text{Power}[\ll 2 \gg] x\right] \right) \right] \right) / \left( \right.$   
 $\left. -1 + e^x \right) \text{Gamma}\left[\frac{1}{2}(-1+d)\right]$  has evaluated to

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In[29]:= Plot[{(doffactor[3]) (EnergyDensity[3, t]), (doffactor[4]) (EnergyDensity[4, t]),  
  (doffactor[5]) (EnergyDensity[5, t]), (doffactor[6]) (EnergyDensity[6, t])}, {t, 0, 10},  
  PlotRange -> {0, 0.354}, AxesLabel -> {"t", "Energy Density"}, PlotLabel -> "Energy Density vs Time"]
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