

this Maple code is a procedure to find the proper divisors of a given positive whole number.

Very exciting

```
ProperDivisors := proc(n);  
  local d, count;  
  count := 0 :  
  for d from 1 to  $\frac{n}{2}$  do  
    if mod(n, d) = 0 then count := count + 1 : print(" One proper divisor of ", n, " is the number ", d);  
    end if;  
  end do;  
  print(" and that is all of them. ");  
  print(" count of proper divisors is ", count);  
end proc;  
proc(n) (1)  
  local d, count;  
  count := 0;  
  for d to 1/2 * n do  
    if mod(n, d) = 0 then  
      count := count + 1; print(" One proper divisor of ", n, " is the number ", d)  
    end if  
  end do;  
  print(" and that is all of them. ");  
  print(" count of proper divisors is ", count)  
end proc  
# Yeah compiles
```

ProperDivisors(3)

```
[>  
      " One proper divisor of ", 3, " is the number ", 1  
      " and that is all of them. "  
      " count of proper divisors is ", 1 (2)
```

```
[> ProperDivisors(19)  
      " One proper divisor of ", 19, " is the number ", 1  
      " and that is all of them. "  
      " count of proper divisors is ", 1 (3)
```

#We see that count of proper divisors for a prime number is always one. By observation.

ProperDivisors(5·7·11·13·17)

```
[>  
      " One proper divisor of ", 85085, " is the number ", 1
```

```

" One proper divisor of ", 85085, " is the number ", 5
" One proper divisor of ", 85085, " is the number ", 7
" One proper divisor of ", 85085, " is the number ", 11
" One proper divisor of ", 85085, " is the number ", 13
" One proper divisor of ", 85085, " is the number ", 17
" One proper divisor of ", 85085, " is the number ", 35
" One proper divisor of ", 85085, " is the number ", 55
" One proper divisor of ", 85085, " is the number ", 65
" One proper divisor of ", 85085, " is the number ", 77
" One proper divisor of ", 85085, " is the number ", 85
" One proper divisor of ", 85085, " is the number ", 91
" One proper divisor of ", 85085, " is the number ", 119
" One proper divisor of ", 85085, " is the number ", 143
" One proper divisor of ", 85085, " is the number ", 187
" One proper divisor of ", 85085, " is the number ", 221
" One proper divisor of ", 85085, " is the number ", 385
" One proper divisor of ", 85085, " is the number ", 455
" One proper divisor of ", 85085, " is the number ", 595
" One proper divisor of ", 85085, " is the number ", 715
" One proper divisor of ", 85085, " is the number ", 935
" One proper divisor of ", 85085, " is the number ", 1001
" One proper divisor of ", 85085, " is the number ", 1105
" One proper divisor of ", 85085, " is the number ", 1309
" One proper divisor of ", 85085, " is the number ", 1547
" One proper divisor of ", 85085, " is the number ", 2431
" One proper divisor of ", 85085, " is the number ", 5005
" One proper divisor of ", 85085, " is the number ", 6545
" One proper divisor of ", 85085, " is the number ", 7735
" One proper divisor of ", 85085, " is the number ", 12155
" One proper divisor of ", 85085, " is the number ", 17017

```

```

" and that is all of them. "

```

```

" count of proper divisors is ", 31

```

(4)

```

> ProperDivisors(5·7)

```

```

" One proper divisor of ", 35, " is the number ", 1

```

```

" One proper divisor of ", 35, " is the number ", 5

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" One proper divisor of ", 35, " is the number ", 7

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```

" and that is all of them. "

```

```

" count of proper divisors is ", 3

```

(5)

↳ # $2^2 - 1 = 3$ so every semi — prime will have three proper divisors.
Given a composite number that is the product of distinct prime numbers,
That is, no prime powers,
So $c = p_1 \cdot p_2 \cdot p_3 \cdot \dots \cdot p_n$ then
count of proper divisors of c is $2^n - 1$. Quite an insight.
we try 5 distinct prime factors and find count to be $31 = 2^5 - 1$
The count is $2^n - 1$ just like Mersenne numbers. Weeee Houray.
That is probably in a textbook somewhere.
Insight by Matt C Anderson
2021